Moment by Integration Example: Find $I_{x} \& I_{y}$



## EXAMPLE

 figure.Given: The shaded area shown in the

Find: The MoI of the area about the x - and y -axes.

Plan: Follow the steps given earlier.
Solve for Ix


## EXAMPLE

(continued)
Solve for Iy

Solve for Ix again using vertical strip

## GROUP PROBLEM SOLVING

Find: $I_{x}$ and $I_{y}$ of the area.
Solve for Ix


## Solve for Iy

## Summary of Mol calculation



Horizontal Strip

$$
\mathrm{I}_{\mathrm{x}}=\int \mathrm{y}^{2} \mathrm{dA}
$$

if base of strip is on $y$-axis

$$
I_{y}=\int(1 / 3) x^{3} d y
$$



Vertical Strip

$$
\mathrm{I}_{\mathrm{y}}=\int \mathrm{x}^{2} \mathrm{dA}
$$

if base of strip is on x -axis

$$
\mathrm{I}_{\mathrm{x}}=\int(1 / 3) \mathrm{y}^{3} \mathrm{dx}
$$

## Parallel-Axis Theorem



## Composite Area Example: Find $\mathrm{I}_{\mathrm{x}}$



| $\#$ | $\boldsymbol{A}_{\boldsymbol{i}}\left(\mathrm{ft}^{2}\right)$ | $\widetilde{\boldsymbol{y}}_{\boldsymbol{i}}(\mathrm{ft})$ | $\overline{\boldsymbol{I}}_{\boldsymbol{i} \boldsymbol{x} \boldsymbol{\prime}}\left(\mathrm{ft}^{4}\right)$ | $\boldsymbol{I}_{\boldsymbol{i} \boldsymbol{x}}\left(\mathrm{ft}^{4}\right)$ |
| :---: | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |
| 2 |  |  |  |  |
| 3 |  |  |  |  |
| 4 |  |  |  |  |

