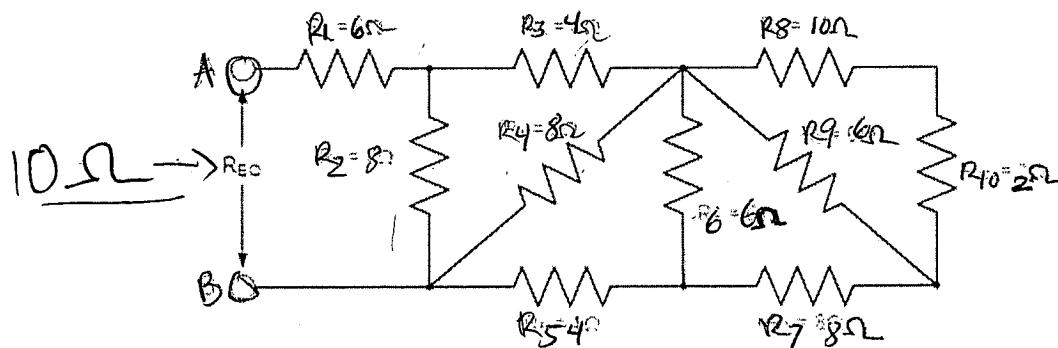
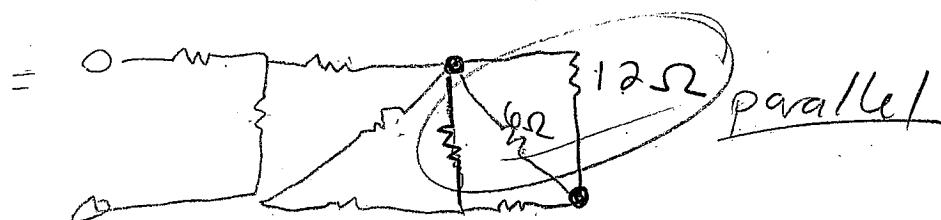


Closed Book. One double sided sheet of notes and a calculator are allowed.

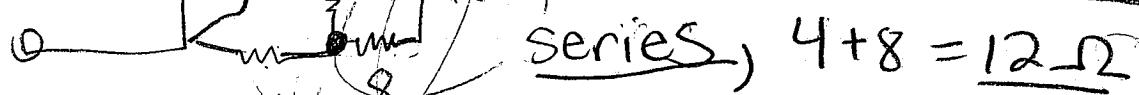
- 1) Find the effective resistance R_{eq} in the network below (it's easier than it may look at first).



$$\begin{aligned} R_8, R_{10} &\rightarrow \text{series} \\ 10 + 2\Omega &= 12\Omega \end{aligned}$$



$$\frac{2}{12} + \frac{1}{12} = \frac{3}{12} \rightarrow 4\Omega$$

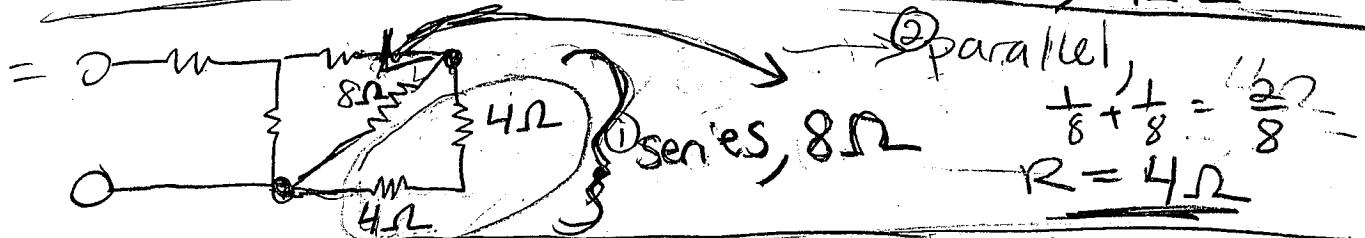


$$4 + 8 = 12\Omega$$



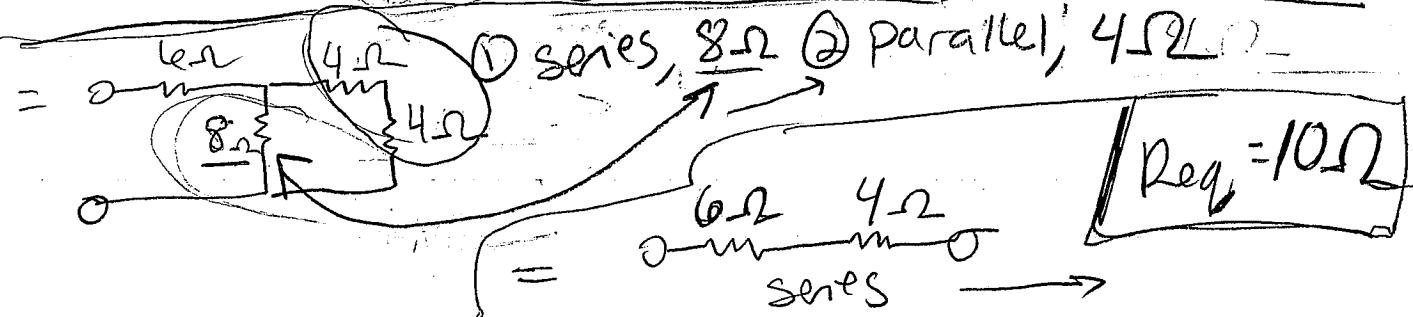
$$\frac{1}{12} + \frac{2}{12} = \frac{3}{12}$$

$$\rightarrow 4\Omega$$



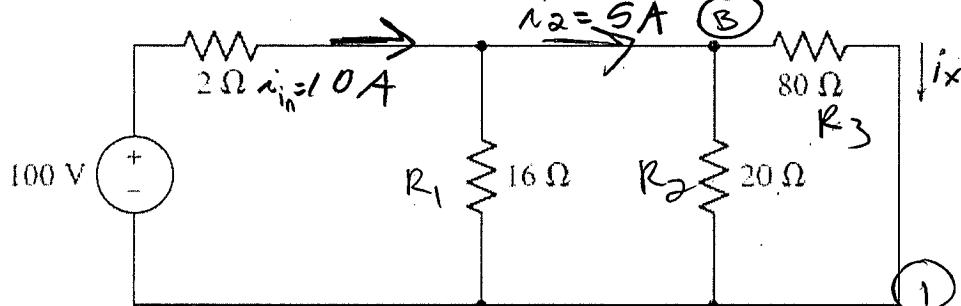
$$\frac{1}{8} + \frac{1}{8} = \frac{2}{8} = \frac{1}{4}$$

$$R = 4\Omega$$



$$R_{eq} = 10\Omega$$

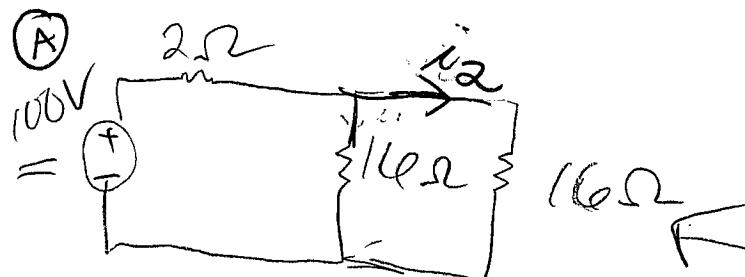
2) Use current division to find the current i_x in the circuit below



① $\frac{R_2, R_3}{\text{parallel}}$

$$\frac{1}{80} + \frac{4}{80} = \frac{5}{80}$$

$$\frac{80}{5} = 16\Omega$$



Ⓑ $i_{in} = 10A$

② $10\Omega = R_{eq}$

$$V = RI \rightarrow I = V/R = \frac{100}{10}$$

$$I_{in} = 10A$$

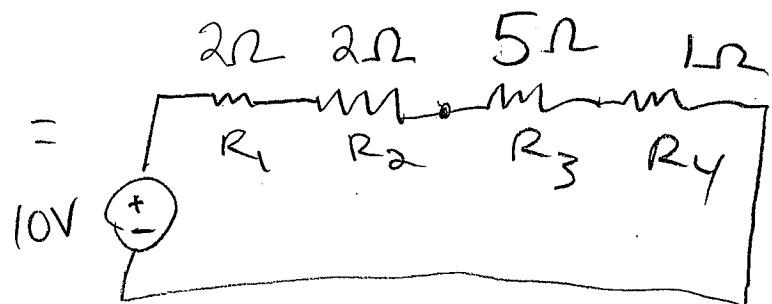
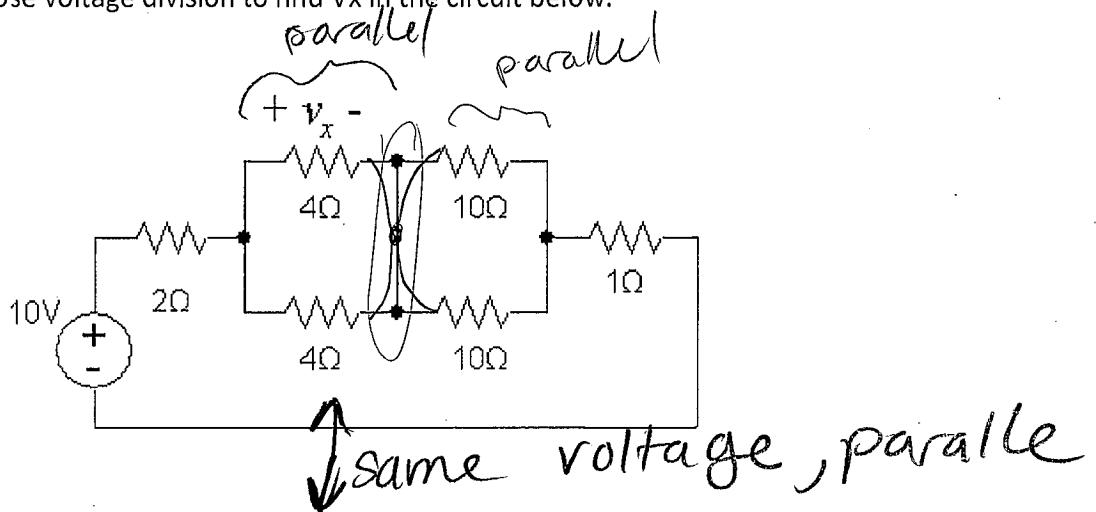
③ Current - divider

Ⓐ $i_2 = i_{in} \left[\frac{R_{11}}{R_1 + R_2} \right] = 10A \left[\frac{16\Omega}{32\Omega} \right] = 5A$

Ⓑ $i_x = i_2 \left[\frac{R_2}{R_2 + R_3} \right] = 5A \left[\frac{20\Omega}{100\Omega} \right] = 1A$

$$i_x = 1.0A$$

- 3) Use voltage division to find V_x in the circuit below.



$$V_x = V_{in} \left[\frac{R_2}{R_1 + R_2 + R_3 + R_4} \right]$$

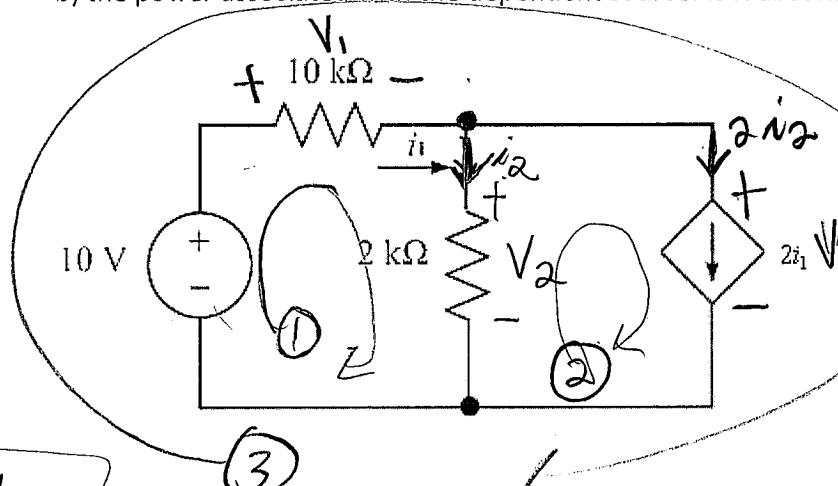
$$= 10V \left[\frac{\frac{2}{2+2+5+1}}{\frac{2}{2+2+5+1}} \right] = \frac{10 \cdot 2}{10}$$

$$\boxed{V_x = 12.0V}$$

4) Find

a) the current $i_1 = 1.25 \text{ mA}$

b) the power associated with the dependent source. Is it absorbing or delivering power?



KCL

$$i_1 = i_2 + 2i_1 \rightarrow i_2 = -i_1$$

$P = -6.25 \text{ mW}$
delivering

$$\begin{aligned} V_3 &= -2.5 \text{ V} \\ P &= +IV \text{ (Passive)} \\ &= -(2)i_1(V_3) \\ &= -(2)(1.25 \text{ mA})(-2.5 \text{ V}) \end{aligned}$$

$P = -6.25 \text{ mW}$
delivering

KVL

$$1) -10V + V_1 + V_2 = 0$$

$$2) -V_2 + V_3 = 0$$

$$3) -10V + V_1 + V_3 = 0$$

OL

$$\begin{aligned} V_1 &= R_1 I_1 = (10k\Omega)i_1 \\ V_2 &= R_2 I_2 = (2k\Omega)i_2 \\ &= (2k\Omega)(-i_1) \end{aligned}$$

$$1) -10V + 10,000i_1 - 2000i_1 = 0 \rightarrow i_1 = \frac{10V}{8000\Omega} = 1.25 \text{ mA}$$

$$2) 2000i_1 + V_3 = 0 \rightarrow V_3 = -2000i_1 = -2k\Omega(1.25 \text{ mA})$$

$$3) -10V + 10,000i_1 + V_3 = 0 \rightarrow V_3 = -2.5 \text{ V}$$

$$i_1 = 1.25 \text{ mA}$$

$$V_3 = -2.5 \text{ V}$$

1.25 mA